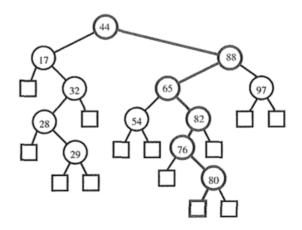
Homework 3 (55pts)

- (a) (5 points) Illustrate the execution of the heap-sort algorithm on the following sequence: (2, 5, 16, 4, 10, 23, 39, 18, 26, 15). Show the contents of the (min) heap and the sequence at each step of the algorithm. Indicate upheap or downheap bubbling where appropriate.
 - (b) (5 points) Illustrate the execution of the bottom-up construction of a (min) heap (like in Figure 2.49) on the following sequence: (2, 5, 16, 4, 10, 23, 39, 18, 26, 15, 7, 9, 30, 31, 40).
- 2. (10 points) Let T be a (min) heap storing n keys. Give the **pseudocode** for an efficient algorithm for printing all the keys in T that are smaller than or equal to a given query key x (which is not necessarily in T). You can assume the existence of a O(1)-time print(key) function. For example, given the heap of Figure 2.41 and query key x = 7, the algorithm should report 4,5,6,7. Note that the keys do not need to be reported in sorted order. Your algorithm should run in O(k) time, where k is the number of keys reported.

Letter	A	В	С	D	E	F	G	Н	Ι	J	K	L	Μ
Key	0	1	2	3	4	5	6	7	8	9	10	11	12
Letter	N	0	Р	Q	R	S	Т	U	V	W	Х	Y	Ζ
Key	13	14	15	16	17	18	19	20	21	22	23	24	25

- 3. Use the table below to convert a character key to an integer for the following questions.
 - (a) (5 points) Give the contents of the hash table that results when the following keys are inserted in that order into an initially empty 13-item hash table: $(E_1, A, S_1, Y, Q, U, E_2, S_2, T, I, O, N)$. Use $h(k) = k \mod 13$ for the hash function for the k-th letter of the alphabet (see above table for converting letter keys to integer values). Use linear probing.
 - (b) (5 points) Give the contents of the hash table that results when the same keys are inserted in that order into an initially empty 13-item hash table. Use $h(k) = k \mod 13$ for the hash function for the k-th letter of the alphabet (see above table for converting letter keys to integer values). Use double hashing and let $h'(k) = 1 + (k \mod 11)$ be the secondary hash function.
- 4. (a) (5 points) Insert into an initially empty binary search tree items with the following keys (in this order): 30, 40, 23, 58, 48, 26, 11, 13. Draw the resulting tree after all insertions.
 - (b) (5 points) Remove from the binary search tree given below the following keys (in this order): 32, 65, 76, 88, 97. Draw the tree after **each** removal.



- (c) (5 points) A different binary search tree results when we try to insert the same sequence into an empty BST in a different order. Give an example of this with at least 5 elements and show the two different binary search trees that result.
- 5. (10 points) Let T be a binary search tree, and let x be a key. Give an efficient algorithm for finding the smallest key y in T such that y > x. Note that x may or may not be in T. Explain why your algorithm has the running time it does.